THE IMPACT OF EXCHANGE RATE DEPRECIATION AND THE MONEY SUPPLY GROWTH ON INFLATION: THE IMPLEMENTATION OF THE THRESHOLD MODEL\textsuperscript{1}

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Abstract

This paper investigates the impact of exchange rate depreciation and money growth to the CPI inflation in Indonesia. Using monthly data from 1980:1 to 2008:12, our econometric evidence shows that there are indeed threshold effects of money growth on inflation, but no threshold effect of exchange rate depreciation on inflation. However the threshold value for exchange rate depreciation is found at 8.4\%, and there is no significant difference between the coefficient both below and above the threshold value. Meanwhile, two threshold values are found for money growth, i.e. 7.1\% and 9.8\%, and they are statistically different. The impact on inflation is high when money grows by up to 7.1\%, it is moderate when money grows by 7.1\% to 9.8\%, and it is low when money grows by above 9.8\%.

JEL Classification: C22; E31; E51.

Keywords: Inflation, Threshold Effect; Indonesia

\textsuperscript{1} Extracted from Wimanda (2010), Doctoral Thesis, Chapter 4, “Threshold Effects of Exchange Rate and Money Growth on Inflation”.

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I. INTRODUCTION

Concerns about inflation have been very intense since Indonesia adopted the inflation targeting in 2000. One of the important topics of the study is to examine the factors that cause inflation.

Wimanda (2010) found that inflation in Indonesia is significantly influenced by inflation expectations (backward-looking and forward-looking), output gap, exchange rate depreciation, and growth in money supply. Analysis of monthly samples from early 1980 until the end of 2008 shows that the formation of inflation expectations in Indonesia is still dominated by the backward-looking inflation expectations with a share of 0.7, while the portion of forward-looking inflation expectations is around 0.2. In his analysis, Wimanda also found that the impact of exchange rate is greater than the impact from the growth in money supply (M1). The analysis assumes that the impact of these two variables is linear, meaning that their impact is constant for each level of exchange rate depreciation and money supply growth.

By using the threshold model, this paper will test whether the impact of exchange rate and money supply growth on inflation is linear or not. And then to test whether there is a threshold value, how much the threshold value that can be identified, and the extent of the impact.

The systematic of this paper is as follows. Literature study will be discussed in the second chapter. Methodology and data will be discussed at the third part of this paper, while the estimation results and conclusions will be presented at the fourth and fifth chapter.

II. THEORY

2.1. Pass-through of Exchange Rate

One of the central issues in international economics is the pass-through of exchange rate which is defined as an impact of 1 percent of depreciation on the domestic inflation. In general, to test the exchange rate pass-through, we estimate the following equation:

\[ \pi_t = \alpha + \gamma e_t + \delta x_t + \epsilon_t \]  

(1)

where \( \pi_t \) is the domestic inflation, \( e_t \) is the depreciation of the exchange rate (nominal), and \( x_t \) is the other control variables (in growth).

In general, the study of exchange rate pass-through can be divided into 3 groups.

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The first group is the study of the impact of exchange rate on the import prices of certain industries, like as conducted by Bernhofen and Xu (1999) and Goldberg (1995). The second group is the study of the impact of exchange rate on import prices in the aggregate, for example Hooper and Mann (1989) and Campa and Goldberg (2005). And the third group is the study of the impact of exchange rate on the CPI or WPI, for example, Papell (1994) and McCarthy (2000).

Although the literature on exchange rate pass-through is very plentiful, but empirical studies mostly focus on developed countries. A survey carried out by Menon (1995) showed that 48 studies on exchange rate pass-through specifically cover the United States and Japan. Similarly, Goldberg and Knetter (1997) mentioned that the study of exchange rate pass-through during the 1980s is dominated by the USA.

For OECD countries, the study of the impact of exchange rate pass-through on their import prices was conducted by Campa and Goldberg (2005). They found that exchange rate pass-through is partial, where import prices reflect 60 percent of exchange rate movements in the short term and nearly 80 percent in the long term. They also found that countries which have a low exchange rate volatility and low inflation have a low impact of exchange rates pass-through.

Using 71 countries data from 1979 to 2000, Choudhri and Hakura (2006) showed that there was a strong positive relationship between the exchange rate pass-through with the inflation average. Countries with low inflation tend to have a low exchange rates pass-through, and vice versa.

The relationship of exchange rate and inflation in Malaysia, Philippines, and Singapore was examined by Alba and Papper (1998) during the Q1 of 1979 Q1 until the Q2 of 1995. They found that the exchange rate pass-through for the Philippines is higher compared to Malaysia, while the exchange rate pass-through to Singapore was oppositely negative.

To support the argument of “fear of floating”, Calvo and Reinhart (2000) also examined a number of developed and developing countries, including Malaysia and Indonesia. By using the monthly data from August 1997 through November 1999, they found the pass-through rate in Indonesia was 0.062.

### 2.2. Relationship between Money and Inflation

The quantity theory and the exchange equation provide a useful framework to analyze empirically the relevance of money in the economy. The relationship of money and inflation can
be derived from the money demand equation. The public wants to hold money to buy goods and services. If the price of goods and services rises, people tend to hold more money. The most important factor in the demand for money is the income. When incomes rise, people will tend to shop more. Higher expenditures are associated with more cash on hand. Thus, this relationship can be written as:

\[
\frac{M}{P} = kY,
\]  

(2)

where \(M\) is the nominal money, \(P\) is the price level based on the CPI or GDP deflator, \(Y\) is the income and \(k\) is the proportion factor. Equation (2) can be rewritten as

\[
P = \frac{1}{k} \frac{M}{Y}
\]  

(3)

By assuming that the causality from \(M\) to \(P\) exists, equation (3) states that the quantity of money determines the price level, although money is not the only factor. For example, when income and other factors which are reflected by \(k\) do not change, and when the quantity of money increases, the price level will increase.

Milton Friedman (1968) argues that inflation is a monetary phenomenon. Studies conducted by Lucas (1980), Dwyer and Hafer (1988), Friedman (1992), Barro (1993), McCandless and Weber (1995), Dewald (1998), Rolnick and Weber (1997) and others concluded that the changes in the quantity of money and price changes have a close relationship.

Dwyer and Hafer (1999) showed that the price level has a positive and proportional relationship to the quantity of money in America, Britain, Japan, Brazil, and Chile during the 20th century. They also showed that in the shorter term, 5 years, the relationship of money growth and inflation remains in force.

Empirical study of the relationship between money growth (M1 and M2) and the inflation in 160 countries was carried out by De Grauwe and Polan (2005). They showed that during the past 30 years, the relationship of money supply growth and inflation is still valid. However, after dividing the sample based on the rate of inflation, they showed that countries with low inflation (below 10%), the relationship between both variables weakened. Conversely, the relationship was strong in the countries with high inflation rates. However, this study did not specify at what level of money supply will give a different effect on inflation.
2.3. Threshold Model Application

Threshold model is a special case of complex statistical frameworks, such as mixture models, switching models, Markov-switching model, and smooth transition threshold model (Hansen, 1997).

Threshold model can be applied in many cases. For example, Galbraith (1996) conducted a study on the relationship between money and output. By using the data of US and Canada, he found that money has a strong influence on the output when the value of money growth is below certain threshold. This result is consistent with the proposition that the monetary policy has little impact or no impact at all on when the money growth is very high.

Khan and Senhadji (2001) investigated the relationship between the inflation and economic growth in 140 countries during the period of 1960 until 1998. They argue that inflation has a negative impact on the economy when inflation is above certain threshold values. In contrast, inflation has a positive impact on the economy when inflation is below the threshold value. They found that the threshold value for developed countries is 1-3 percent, and about 11-12 percent of threshold value for developing countries.

Threshold model is also used by Papageorgiou (2002) to evaluate the level of openness of the economy. Foster (2006) examined the relationship of export and economic growth for African countries. The evaluation of the fiscal deficit was also performed using the threshold models, for example for the case of USA (see Arestis, Cipollini and Fattouh, 2004) and Spain (see Bajo-Rubio, Diaz-Roldan and Esteve, 2004).

Meanwhile, the study of the threshold of exchange to the inflation and the threshold of money supply to inflation, to our knowledge, does not yet exist. Therefore, this study is conducted with the intention to complete the literature gap.

III. METHODOLOGY

3.1. Empirical Model and the Estimation Technique

This study is using the threshold model to answer the questions above. Threshold model is a special case of a complex statistical framework, such as mixture models, switching models, Markov-switching models, and smooth transition threshold models. In general, the threshold model can be written as follows:

\[ y_t = \beta' x_t + \delta_1 z_t I(t h_t \leq \lambda) + \delta_2 z_t I(t h_t > \lambda) + \mu_t \]  

(4)
where is the dependent variable, is the explanatory variable to be tested, is the vector of other
explanatory variables, is the indicator function, is a threshold variable, and is the value of the
threshold. In the equation above, the observations are divided into two regimes; depend on
whether the threshold variable is smaller or larger than the value of.

To estimate the model, the threshold value and the value of slope parameter are estimated
simultaneously. Hansen (1997) recommended seeking estimates of by finding the minimum
value of sum of squared errors. To ensure that the number of observations in each regime is
sufficient, the models are estimated for all the threshold value from the variable threshold
between the 10th and 90th percentile.

Having found the threshold value, we need to test whether the value is statistically
significant or not. In this case, whether the null hypothesis is to be rejected or accepted. One
thing that may complicate is the non-identified threshold value in the null hypothesis. This
implies that the classical test does not have a standard distribution, so that critical values cannot
be obtained from the standard distribution tables.

This study follows Hansen (1997, 2000) in the search for multiple regimes in the data by
using the exchange rate depreciation and the growth of M1 as the threshold variable. This
method, which is based on the asymptotic distribution, will test the significance of regimes
selected by the data.

In this study, we do not evaluate long-term relationship of the value of the exchange rate
and the money supply to the price level, but we are more interested to see the short-term
relationship of the exchange rate depreciation and the money supply growth to inflation. To
examine the existence of a threshold effect of exchange rate depreciation on inflation, this
hybrid model of Phillips curve will be estimated as follows:

\[
\pi_t = c + \alpha_1 \pi_{t-1} + \alpha_2 \pi_{t+1}^e + \beta \text{gap}_t + \gamma_1 (1 - d_t) [(er)_t I (er_t > er*)] \]
\[
+ \gamma_2 d_t [(er)_t I (er_t \leq er*)] + \theta m_t + \delta_1 \text{crisis} + \delta_2 \text{fuel} + \delta_3 \text{fitri} + \epsilon_t
\]

where,
\[
d_t = \begin{cases} 
1 & \text{if } er_t \leq er* \\
0 & \text{if } er_t > er*
\end{cases}
\]

is inflation, \(\pi_{t-1}\) is the backward-looking inflation expectations, \(\pi_{t+1}^e\) is the forward-looking
inflation expectations, \(\text{gap}_t\) is the output gap, \(er_t\) is the depreciation of the exchange rate\(^4\), \(er^*\)

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\(^4\) The exchange rate is defined as the domestic currency per foreign currency. In this case we use Rp/USD. Thus, a negative er value
means depreciation, while a positive er value indicates an appreciation.
is the threshold value of the exchange rate, \( m_t \) is the growth of money supply (M1), \( \text{crisis} \) is the dummy variable to capture the financial crisis 1997-1998, \( \text{fuel} \) is a dummy variable to capture the fuel price surge in January 2005 and October 2005, and \( \text{fitri} \) is the dummy variable to capture the phenomenon of Idul Fitri.

We use instrumental variables (IV) estimators, which is the two-stage least squares (TSLS). This estimation method can overcome the endogeneity problems given that within the model used there is then inflation value in the future.

Model estimation is done by conditional least squares method which can be explained as follows:

For each threshold value \( \text{er}_t^* \), the model is estimated through TSLS, to obtain the sum of squared residuals (SSR). The least squares estimation of \( \text{er}_t^* \) is obtained by choosing the threshold value \( \text{er}_t^* \) which has the minimum value of SSR. If we put all the threshold value observations into the vector, the compact notation of equation (2) then is as follows:

\[
y = x\beta_{er} + \epsilon, \; \text{er} = \underline{er}, \ldots, \overline{er},
\]

where \( \beta_{er} = (\alpha_1 \alpha_2 \beta \gamma_1 \gamma_2 \theta \delta_1 \delta_2 \delta_3)^\prime \) is the vector of parameters, \( y \) is the dependent variable, and \( x \) is the matrix of the explanatory variables. It is noteworthy that the coefficient vector \( \beta \) is indexed with \( \text{er} \) to show its dependence to the threshold value, which ranged from \( \underline{er} \) to \( \overline{er} \). We define \( S_1(\text{er}) \) as SSR with the threshold value of exchange rate depreciation on \( \text{er} \). The threshold estimation value \( \text{er}_t^* \) which is obtained is the threshold value with the minimum \( S_1(\text{er}) \) value, namely:

\[
\text{er}_t^* = \text{argmin} \{ S_1(\text{er}), \text{er} = \underline{er}, \ldots, \overline{er} \}
\]

Once the threshold value is obtained, we need to examine whether the threshold effect is statistically significant or not. In equation (2), to test the existence of the threshold effect, we need to test the null hypothesis, which is \( H_0 : \gamma_1 = \gamma_2 \). Hansen (1997, 2000) suggested the bootstrap method to simulate the asymptotic distribution of the likelihood ratio test from the \( H_0 \) as the following:
$$LR_0 = n \frac{(S_0 - S_1)}{S_1},$$  

(8)

where $S_0$ and $S_1$ is the SSR for $H_0: \gamma_1 = \gamma_2$ and $H_1: \gamma_1 = \gamma_2$. In other words, $S_0$ and $S_1$ is the SSR from the equation (2) without and with the threshold effects. Asymptotic distribution of $LR_0$ is non-standard and dominate the distribution of $\chi^2$. The distribution of generally depends on the moments of sample, so that the critical values cannot be tabulated.

Given that $\gamma$ has not been identified, the asymptotic distribution of $LR_0$ is not $\chi^2$. Hansen (1997) showed that this can be approximated by using the following bootstrap procedure:

1. Set $\mu_t^*, t = 1, \ldots, n$ as random number, drawn from a normal distribution whose mean is zero and whose variance is one i.e. $N(0,1)$.
2. Set $y_t^* = \mu_t^*$.
3. By using the observation of $x_t, t = 1, \ldots, n$, regress $y_t^*$ at $x_t$ and find the residual variance $\bar{\sigma}^2_n$ from the linear model, where $\bar{\sigma}^2_n = \frac{1}{n} \sum_{t=1}^{n} (y_t^* - x_t \bar{\beta})^2$.
4. By using the observation of $x_t, t = 1, \ldots, n$, regress $y_t^*$ at $x_t(\gamma)$ and find the residual variance $\bar{\sigma}^2_n(\gamma)$ from the threshold model, where $\bar{\sigma}^2_n(\gamma) = \frac{1}{n} \sum_{t=1}^{n} (y_t^* - x_t(\bar{\beta}_c))^2$ and $\gamma$ are the threshold value.

5. Calculate $F_n^*(\gamma) = n \left( \frac{\bar{\sigma}^2_n - \bar{\sigma}^2_n(\gamma)}{\bar{\sigma}^2_n(\gamma)} \right)$.

6. Repeat step number 4 and 5 for the other $\gamma$.

7. Find $F_n^* = \sup_{\gamma \in \Gamma} F_n^*(\gamma)$.

8. Repeat step 1 to 7 over and over again.

Hansen (1997) also showed that the repetitive sampling from $F_n^*$ can be used as an approximation to the asymptotic distribution from $F_n$. The $p$-value of this test is to calculate the percentage of bootstrap samples whose the value of $F_n^*$ exceeds $LR_0$ (see equation (5)).
This study follows Hansen (2000) in forming the confidence region for \( er^* \). The confidence intervals for the threshold parameter inversion are built by inverting the asymptotic distribution of the likelihood ratio statistics. In this case, we tested null hypothesis \( H_0: \ er^* = er \) by calculating the likelihood test as follows:

\[
LR(er) = n \frac{S_1(er) - S_1(er^*)}{S_1(er^*)},
\]

(9)

where \( S_1(er) \) and \( S_1(er^*) \) is the SSR from equation (2) with threshold \( er \) and \( er^* \). Define \( c_\xi(\beta) \) as the \( \beta \)-level critical value for \( \xi \) from Table 1 in Hansen (2000). Thus that defines

\[
\hat{\Gamma} = [er : LR(er) < c_\xi(\beta)]
\]

(10)

Hansen (2000) shows that \( LR(er) \) is asymptotically valid for \( \beta \)-level confidence at \( er \). To get a confidence interval, we plot the likelihood ratio \( LR(er) \) with the threshold value \( (er) \), pull a straight line on \( c_\xi(\beta) \), and mark the threshold value with the likelihood ratio whose value is under the critical value. It should be noted that the \( LR(er) \) will be equal to zero when \( er = er^* \).

To test the existence of threshold effect of the money growth toward inflation, we use the same model, but we replace the exchange rate depreciation with the growth of money supply as the threshold variable. The model will be next estimated as follows:

\[
\pi_t = c + \alpha_1 \pi_{t-1} + \alpha_2 \pi_{t-1}^e + \beta \text{gap}_t + \gamma e_{rt} + \theta_1 (1 - d_t) \left( (m_t) I (m_t > m^*) \right) + \theta_2 d_t \left( (m_t) I (m_t \leq m^*) \right) + \delta_{\text{crisis}} + \delta_{\text{fuel}} + \delta_{\text{fitri}} + \varepsilon_t
\]

(11)

where

\[
d_t = \begin{cases} 
1 & \text{if } m_t \leq m^* \\
0 & \text{if } m_t > m^*
\end{cases}
\]

Meanwhile the estimation and testing procedures for threshold growth of money supply is the same as the procedure above.

3.2. Data

We use CPI data, output gap, exchange rate, and M1. These data is obtained from Bank Indonesia (BI) and BPS. For the analysis, we use the monthly data from 1980 to 2008 (see Table 1).
IV. RESULT AND ANALYSIS

4.1. Threshold Effect on the Exchange Rate Depreciation

Table 3 below shows the results of TSLS estimation of the equation (2) without the presence of threshold effect (by setting $\gamma_1 = \gamma_2$). From this table we can see that all the parameters are significant, except for constant. By using the adjusted HP filter as a proxy in the calculation of potential output, we find that the coefficient of exchange rate depreciation (yoy) is -0.050 and the coefficient of M1 growth is 0.021. These results show that in average the impact of exchange rate depreciation on inflation is still greater than the impact of the money supply growth.
To estimate the threshold of exchange rate depreciation, we use equation (2). The threshold value in search has a value ranging from -30% to 0%. With an increase of 0.06% there are 500 candidates of the threshold value. From these 500 threshold values, the lowest SSR value is 408.25, at the level of 8.4%. This means that the threshold depreciation amounted to 8.4%.

Table 4 shows the results of model estimation using the adjusted HP filter to calculate the potential output. From the table we can see that the impact of exchange rate depreciation on inflation, when the level of depreciation is greater than or equal to 8.4%, is for 0.056, while the impact, when the exchange rate depreciation rate is below 8.4%, is 0.045. Both coefficients above are significant at the level of 1%.

The horizontal line in Figure 1 shows the 90% of confidence interval. The area below the horizontal line forms the region of acceptance. The LR(g) statistic will be nil at the optimal threshold. From the figure we can see that the confidence interval for the threshold exchange rate is too wide. The area below the line where \( LR(g) = 5.94 \) has the value ranging from -23.52% to -2.64%. This shows that the estimation of threshold value effect for the exchange rate depreciation is not too accurate.

To test whether there is a difference between a linear and a threshold model, we performed 1000 times bootstrapping. We followed the procedure suggested by Hansen (1997) to yield the critical value.

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5 This is the critical value for 90% confidence interval from Table 1 Hansen (2000).
It was found that most of the $F_{\text{gap}}$ are superior to the value of $F_{\alpha}$, which is -12.12, where the $p$-value is 0.957. This shows that we cannot reject the null hypothesis where $\gamma_1 = \gamma_2$. Thus, it can be concluded that there was no significant difference in the impact of the exchange rate depreciation on inflation at the level below and above the threshold. In other words, the impact of exchange rate depreciation on inflation is linear, that is equal to 0.05% for every 1% of depreciation rate.

As for the robustness check, we use various alternative models, which are the model by that use the peak-to-peak output gap and model by adopting asymmetric ties between inflation and output, which is the L-shaped function\(^6\). This alternative model can be seen in Table 5.

Table 6 shows the estimation results with and without the threshold effect. From this table we can see that the coefficient of the exchange rate depreciation is below or equal to its

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### Table 5.

<table>
<thead>
<tr>
<th>Model</th>
<th>Output Gap Measurement</th>
<th>Output Gap Function</th>
<th>ER Dep.Threshold</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Peak-to-Peak</td>
<td>Linear</td>
<td>No</td>
</tr>
<tr>
<td>2</td>
<td>Peak-to-Peak</td>
<td>Linear</td>
<td>Yes</td>
</tr>
<tr>
<td>3</td>
<td>Adjusted HP Filter</td>
<td>Non-Linear</td>
<td>No</td>
</tr>
<tr>
<td>4</td>
<td>Adjusted HP Filter</td>
<td>Non-Linear</td>
<td>Yes</td>
</tr>
</tbody>
</table>

\(^6\) According to the results of the 3rd chapter of the Doctoral Thesis of Wimanda (2010), the Phillips curve in Indonesia is more suited to be modeled with the L-shape function with wall parameter of 8.5%. This function is actually a parabolic function where the impact of the output gap to inflation would be enormous if the output gap is close to 8.5%.
Table 6. Robustness check for Phillips curve with the threshold of exchange rate depreciation

<table>
<thead>
<tr>
<th>Variable</th>
<th>Model-1</th>
<th>Model-2</th>
<th>Model-3</th>
<th>Model-4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant</td>
<td>0.007 (0.186)</td>
<td>0.011 (0.192)</td>
<td>-0.325*** (0.122)</td>
<td>-0.358*** (0.127)</td>
</tr>
<tr>
<td>Inflation (-1)</td>
<td>0.714*** (0.043)</td>
<td>0.730*** (0.048)</td>
<td>0.694*** (0.037)</td>
<td>0.705*** (0.041)</td>
</tr>
<tr>
<td>Inflation(1)</td>
<td>0.223*** (0.059)</td>
<td>0.199*** (0.067)</td>
<td>0.249*** (0.051)</td>
<td>0.233*** (0.056)</td>
</tr>
<tr>
<td>Output Gap Linear (-9)</td>
<td>0.071** (0.03)</td>
<td>0.081** (0.032)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Output Gap Non-Linear(-9)</td>
<td>-0.048*** (0.009)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Exchange Rate Dep(-1)</td>
<td>-0.048*** (0.009)</td>
<td>-0.057*** (0.013)</td>
<td>-0.047*** (0.009)</td>
<td>-0.054*** (0.011)</td>
</tr>
<tr>
<td>Threshold &lt;= Exchange Rate Dep(-1)</td>
<td></td>
<td>-0.041*** (0.009)</td>
<td></td>
<td>-0.041*** (0.009)</td>
</tr>
<tr>
<td>M1 Growth(-2)</td>
<td>0.027*** (0.008)</td>
<td>0.030*** (0.009)</td>
<td>0.027*** (0.008)</td>
<td>0.031*** (0.008)</td>
</tr>
<tr>
<td>Dummy Crisis</td>
<td>1.228** (0.536)</td>
<td>1.154** (0.547)</td>
<td>0.652 (0.405)</td>
<td>0.462 (0.422)</td>
</tr>
<tr>
<td>Dummy Fuel</td>
<td>2.944*** (0.683)</td>
<td>2.973*** (0.693)</td>
<td>2.772*** (0.648)</td>
<td>2.805*** (0.665)</td>
</tr>
<tr>
<td>Dummy Fitri</td>
<td>0.551** (0.215)</td>
<td>0.548** (0.218)</td>
<td>0.554** (0.208)</td>
<td>0.554** (0.213)</td>
</tr>
<tr>
<td>Adjusted R-squared</td>
<td>0.991</td>
<td>0.991</td>
<td>0.992</td>
<td>0.991</td>
</tr>
<tr>
<td>S.E. of regression</td>
<td>1.103</td>
<td>1.116</td>
<td>1.066</td>
<td>1.091</td>
</tr>
<tr>
<td>SSR</td>
<td>400.161</td>
<td>408.247</td>
<td>373.986</td>
<td>390.569</td>
</tr>
</tbody>
</table>

Threshold ER                       | -8.40            | -8.40            |                  |                  |

p-value                            | 0.999            |                  |                  |                  |

Remarks:
- The number between parentheses is the error standard.
- ***, **, and * indicate the significance level at the level of 1%, 5%, and 10%.

threshold value ($\gamma_1$). And above its threshold value in model 2 and model 4 ($\gamma_2$) the value is negative and significant. We found that the threshold value is equal to the threshold value on the previous model, at the level of -8.4%. Coefficient value $\gamma_1$ is in the range of -0.054 to -0.057, while the coefficient value of $\gamma_2$ is relatively the same at -0.041.

After performing as much as 1,000 times bootstrapping, model 2 and model 4 yield the same conclusion with the main model. Overall, from the bootstrap test statistics, there is not any statistical significance on these variables. The $p$-values range between 0.966 and 0.999. This implies that there is no significant difference between the impact of exchange rate depreciation on inflation, above and below its threshold value.
If we compare model 1 and model 2, as well as model 3 and model 4, we can see that the value of SSR for the threshold model is greater than the value of the SSR on the linear model. This confirms the above conclusion.

![Figure 2. The impact of exchange rate depreciation on the inflation: an illustration](image)

Figure 2 above illustrates the impact of exchange rate depreciation on inflation. From this picture, we can see that the slope in solid blue line is the same for every point. This linear impact (solid blue line) is more preferable than the non-linear impact of (dashed brown line).

4.2 Threshold Effect on the Money Growth

To estimate the threshold value for the money supply growth, we use equation (8) with the output gap, which is calculated based on the adjusted HP filter. This search for the threshold value starts from 0% to 40%, with an increase of 0.08. This means that there are approximately 500 candidates for the threshold value. We found that the threshold value for the M1 growth was 9.84%.

Table 7 shows the estimation results of threshold with using the adjusted HP filter as a measurement of the output gap. Given that the results of the main variables are quite robust, that all coefficients are statistically significant, we can then immediately analyze its threshold results. From the table, the coefficient of the money supply growth, below or equal to 9.84% (\( \theta_1 \)), is 0.099, while the coefficient of the money supply growth above 9.84% (\( \theta_2 \)) is 0.032. Both coefficients are significant at the level of 1%.

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7 This value give the smallest SSR.
The Impact of Exchange Rate Depreciation and the Money Supply Growth on Inflation: the Implementation of the Threshold Model

This result implies that there are differences in the impact of the M1 growth on inflation, above or below its threshold value at 9.84%. As an illustration, shall M1 grow by 5% this month, and then there will be an additional inflation of 0.5% in two months to come. Meanwhile, shall M1 grow 10% this month; there will be then an additional average inflation of 0.98% within 2 months.

Once the threshold value is identified, the next important question is how accurate are these estimates. This requires the calculation of the confidence regions around the threshold value. Figure 3 illustrates the value of likelihood ratio and the threshold value, as well as 90%
confidence intervals. As explained above, the confidence region is calculated by taking the values of $M1$ growth where the value of $LR(M1)$ is below the horizontal line. From this figure it shows that the confidence interval for the money growth is quite narrow, around 7.12% - 10%. This indicates that the estimated threshold value is accurate enough.

The next step is to test whether the threshold value exists by performing bootstrapping. By generating new samples, repeated by 1,000 times for the percentile estimation of the asymptotic null distribution $F_n^*$, we find that the $p$-value is 0.001. Thus, the null hypothesis (linear model) can be rejected and it concludes that there is a threshold value for the $M1$ growth.

After finding the first threshold value, we seek the possibility of another threshold value. We can find three regimes at the same time, but this would be very inefficient in terms of computation time. Chong (1994) and Bai (1997) showed that the sequential estimation is consistent, so that it can avoid the problem of calculation. This means that we can fix the first threshold figure, en then seek the second one by assuming that the first threshold is already fixed.

We begin by considering the possibility of another threshold value between 9.84% and 40%. With a value addition by 0.075 there are 400 candidates for the threshold value. It is found that the smallest SSR is when the threshold is at 17.13%. This means that 17.3% is the second threshold candidate. TSLS estimation results can be seen in Table A (see Appendix). Although these entire $M1$ growth coefficients are significant at level of 1%, but after conducting the bootstrapping, we found the $p$-value at 0.177 which is slightly larger than 10%. Thus, the null hypothesis from these 2 threshold regime cannot be rejected. In other words, the relationship between inflation and the $M1$ growth is linear by the time $M1$ grows above 9.84%.

The next effort to search the threshold candidate is between 0% and 9.84%. We selected 350 values and found the minimum SSR at the point of 7.08%. TSLS Estimation results with 2 thresholds: 9.84% and 7.08% can be seen in Table 8. From the table we can note that the coefficient of $M1$ growth, when it grows under 7.08%, is 0.146; when it grows between 7.08% and 9.84%, the coefficient is 0.088, and when it grows over than 9.84%, the coefficient
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decreases to 0.033. All of the above coefficients are significant at the level of 1%. This shows that a higher M1 growth of M1, will cause less impact on the inflation.

Figure 4 shows that the minimum likelihood ratio is found at the threshold point of 7.08%. Its 90% confidence interval is quite narrow, which is from 6.94% to 8.04%. This indicates that 7.08% is a potential candidate for the second threshold.

A formal test is carried out by bootstrapping samples. By replicating samples and repeating it by 1,000 times, we find the p-value at 0.004. Thus, we reject the null hypothesis of the 2 regimes. Based on these tests, we conclude that there are 3 threshold regimes for the M1 growth.
Next we look for another threshold value candidate between 0% and 7.08%. With an addition of 0.028%, we evaluated 250 candidates. Of the 250 these candidates, we found that the SSR value is the lowest at the point of 4.93%.

Table B (see Appendix) presents the TSLS estimation result with four regimes. All coefficients are significant, except the coefficient for M1 growth from 0% to 4.93% \((p\text{-value} = 0.273)\). The formal testing through bootstrapping produces p-value by 0.191. This indicates that the relationship of inflation with the M1 growth is linear when M1 grows between 0% and 7.12%. Given that the third threshold is not significant, it is impossible to separate further the samples.

### Table 9.
**Alternative model for the threshold of M1 growth**

<table>
<thead>
<tr>
<th>Model</th>
<th>Output Gap Measurement</th>
<th>Output Gap Function</th>
<th>M1 Threshold</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>Peak-to-Peak</td>
<td>Linear</td>
<td>No</td>
</tr>
<tr>
<td>6</td>
<td>Peak-to-Peak</td>
<td>Linear</td>
<td>Yes</td>
</tr>
<tr>
<td>7</td>
<td>Adjusted HP Filter</td>
<td>Non-Linear</td>
<td>No</td>
</tr>
<tr>
<td>8</td>
<td>Adjusted HP Filter</td>
<td>Non-Linear</td>
<td>Yes</td>
</tr>
</tbody>
</table>

As for robustness check, again we use a variety of models with the difference that lies in the measurement of the output gap and the non-linear Phillips curve. Table 9 shows the difference.

As shown in Table 10, these empirical results yield some interesting results. First, all coefficients, except the constant and dummy variables for the crisis on some models, are significant. Second, the estimation of the threshold value is the same, 9.84% and 7.08%. Third, the coefficient of the threshold effect is somewhat different, yet the difference is abysmal. The coefficient of M1 growth when growing under 7.08% ranges from 0.156 to 0.160; coefficient of M1 growth when growing between 7.08% and 9.84% ranges from 0.094 to 0.096, and the coefficient of M1 growth when growing over 9.84% ranges from 0.035 to 0.037.

Given that all the \(p\)-values of the bootstrapping are less than 1%, then we can reject the null hypothesis for the two regimes and prefer to the three regimes. In addition, when compared to the SSR value to the threshold model (model 6 and model 8) and the SSR value on the linear model (model 5 and model 7), we found that the threshold model is better than the linear model.
**Table 10:**
**Robustness check for the threshold of M1 growth**

<table>
<thead>
<tr>
<th>Variable</th>
<th>Model-1</th>
<th>Model-2</th>
<th>Model-3</th>
<th>Model-4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant</td>
<td>0.062 (0.187)</td>
<td>-0.284 (0.183)</td>
<td>-0.279*** (0.12)</td>
<td>-0.559*** (0.137)</td>
</tr>
<tr>
<td>Inflation (-1)</td>
<td>-0.714*** (0.043)</td>
<td>0.689*** (0.039)</td>
<td>0.694*** (0.037)</td>
<td>0.672*** (0.034)</td>
</tr>
<tr>
<td>Inflation(1)</td>
<td>0.223*** (0.059)</td>
<td>0.250*** (0.053)</td>
<td>0.251*** (0.051)</td>
<td>0.273*** (0.047)</td>
</tr>
<tr>
<td>Output Gap Linear(-9)</td>
<td>0.074** (0.03)</td>
<td>0.060 (0.028)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Output Gap Non-Linear(-9)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Exchange Rate Dep(-1)</td>
<td>-0.048*** (0.009)</td>
<td>-0.043*** (0.008)</td>
<td>-0.047*** (0.009)</td>
<td>-0.042*** (0.008)</td>
</tr>
<tr>
<td>M1 Growth(-2)</td>
<td>0.024*** (0.007)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>M1 Growth(-2) &lt;= 2nd Threshold</td>
<td></td>
<td>0.156*** (0.049)</td>
<td></td>
<td>0.160*** (0.048)</td>
</tr>
<tr>
<td>2nd Threshold &lt; M1 Growth(-2) &lt;= 1st Threshold</td>
<td></td>
<td>0.096*** (0.031)</td>
<td></td>
<td>0.094*** (0.03)</td>
</tr>
<tr>
<td>1st Threshold &lt; M1 Growth(-2)</td>
<td></td>
<td>0.035*** (0.008)</td>
<td></td>
<td>0.037*** (0.008)</td>
</tr>
<tr>
<td>Dummy Crisis</td>
<td>1.235** (0.539)</td>
<td>1.122*** (0.503)</td>
<td>0.644 (0.406)</td>
<td>0.633 (0.386)</td>
</tr>
<tr>
<td>Dummy Fuel</td>
<td>2.929*** (0.685)</td>
<td>2.968*** (0.65)</td>
<td>2.752*** (0.649)</td>
<td>2.819*** (0.619)</td>
</tr>
<tr>
<td>Dummy Fitri</td>
<td>0.550** (0.216)</td>
<td>0.608*** (0.205)</td>
<td>0.553*** (0.209)</td>
<td>0.611*** (0.199)</td>
</tr>
<tr>
<td>Adjusted R-squared</td>
<td>0.991</td>
<td>0.992</td>
<td>0.992</td>
<td>0.992</td>
</tr>
<tr>
<td>S.E. of regression</td>
<td>1.107</td>
<td>1.045</td>
<td>1.070</td>
<td>1.014</td>
</tr>
<tr>
<td>SSR</td>
<td>403.146</td>
<td>357.419</td>
<td>376.347</td>
<td>336.461</td>
</tr>
<tr>
<td>1st Threshold</td>
<td></td>
<td>9.84</td>
<td></td>
<td>9.84</td>
</tr>
<tr>
<td>2nd Threshold</td>
<td></td>
<td>7.08</td>
<td></td>
<td>7.08</td>
</tr>
<tr>
<td>p-value</td>
<td>0.005</td>
<td></td>
<td>0.005</td>
<td></td>
</tr>
</tbody>
</table>

**Remarks:**
- The number within the parentheses is the error standard.
- ***, **, and * indicates the significance level on the level of 1%, 5%, and 10%.

From the test results and analysis above, these empirical results provide strong evidence that the relationship of M1 growth and inflation can be described by three regimes. Figure 5 illustrates this relationship. From the picture, we can see that the slope of the solid brown line when M1 grows up to 7.1% is steeper than the line when M1 grows between 7.1% - 9.8%. Similarly, when M1 grows more than 9.8%, the slope becomes more gently sloping.
V. CONCLUSION

This paper contributes to existing literature in which the threshold determination is done by using the techniques developed by Hansen (1997, 2000). Compared with the definition of threshold conducted arbitrarily, this technique provides some benefits where the threshold value can be determined by the characteristics of the data itself. Furthermore, this technique allows detecting the possibility of other threshold value. If there is only one threshold value fixed one, while in fact there are more than one, then the value of the coefficient can be under/over estimate.

This paper provides a comprehension of the threshold effect of exchange rate depreciation and the growth of money supply (M1) toward the inflation in Indonesia. By using the monthly data from 1980:01 to 2008:12, this model provides strong evidence that there is a threshold effect from the money supply growth on inflation, but it does not find any threshold effect between the exchange rate depreciation and inflation.

All experiments carried out as much as 1,000 times. By using two different output gap measurements, which are the adjusted HP filter and the peak-to-peak method, and two types of inflation-output relationship, which are the linear and L-shape function, our conclusions remain the same. Threshold value of the exchange rate depreciation is 8.4%. However, the coefficient from the exchange rate depreciation at the rate below 8.4% (γ) and the coefficient of the exchange rate above 8.4% (γ2) does not differ much. The F-test gives a conclusion that there is no significant difference between γ and γ2. Thus, the impact of exchange rate depreciation on inflation is linear for all depreciation rates (which is 0.05).

For the growth of money supply, we find the evidence that there are two threshold values, at 7.1% and 9.8%. The F-test concludes that the effect of these three regimes is
significantly different. This empirical result indicates that the impact of money supply growth on inflation is not linear. The biggest impact on money supply growth is between 0% and 7.1% (i.e. 0.15), moderate impact occurs when the money supply to grow between 7.1% and 9.8% (i.e. 0.09), and the lowest impact is when the money supply grows above 9.8% (i.e. 0.03). As the money supply grows higher, the impact on inflation will be reduced.

In general, our findings are in line with Galbraith’s (1996) who studied the relationship between money supply with output. He discovered that money has a great impact on output if the money supply grows below its threshold value as compared when it grows above the threshold. These findings are consistent with the proposition that monetary policy has little or even no effect when the money supply grows very highly.

These findings provide the conclusion that the impact of money supply on inflation when the money supply grows below 9.8% will be greater than the impact of exchange rate depreciation on inflation. This conclusion is different from previous studies that did not include the threshold effect, where the impact of exchange rate depreciation on inflation is greater than the money supply growth at every level.

Although the impact of exchange rate depreciation on inflation is linear, it does not mean that, as the monetary authority, Bank Indonesia can override the depreciation rate because of the impact is moderate. Furthermore, this study suggests that Bank Indonesia should consider the growth of money supply, in this case M1, considering that the impact of M1 is large enough at the time it is at a level below the its threshold value. Although the impact of M1 growth on inflation is not linear with a smaller impact at the time the M1 growth is over its threshold value, this study does not suggest leaving M1 to grow rapidly.

Our findings above are based on the methodology proposed by Hansen (1997, 2000). However, this study does not explain why higher money supply growth gives a mild impact on inflation. Thus, further studies in the future in this area are needed to explain the reason for this asymmetric effect.

The analysis above is based on partial analysis, using a single equation model, despite the fact that the exchange rate and the money supply are not independent. The use of a more complex model where the exchange rate and money supply are used as endogenous variables to evaluate the threshold value, as found in this study, would be an interesting study. It is worth to be reserved for further study.
REFERENCES


### Appendix

#### Table A.
**Phillips curve with the threshold of M1 growth: second point above**

<table>
<thead>
<tr>
<th>Coef</th>
<th>Std. Error</th>
<th>t-Statistic</th>
<th>Prob.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant</td>
<td>-0.571</td>
<td>0.190</td>
<td>-3.000</td>
</tr>
<tr>
<td>Inflation(-1)</td>
<td>0.689</td>
<td>0.0371</td>
<td>8.537</td>
</tr>
<tr>
<td>Inflation(1)</td>
<td>0.248</td>
<td>0.052</td>
<td>4.751</td>
</tr>
<tr>
<td>Output Gap(-9)</td>
<td>0.052</td>
<td>0.021</td>
<td>2.447</td>
</tr>
<tr>
<td>Exchange Rate Dep(-1)</td>
<td>-0.045</td>
<td>0.009</td>
<td>-5.302</td>
</tr>
<tr>
<td>M1 Growth(-2) &lt;= 9.84%</td>
<td>0.127</td>
<td>0.035</td>
<td>3.502</td>
</tr>
<tr>
<td>9.84% &lt; M1 Growth(-2) &lt;= 17.13%</td>
<td>0.057</td>
<td>0.018</td>
<td>3.079</td>
</tr>
<tr>
<td>17.13% &lt; M1 Growth(-2)</td>
<td>0.038</td>
<td>0.009</td>
<td>3.977</td>
</tr>
<tr>
<td>Dummy Crisis</td>
<td>1.219</td>
<td>0.508</td>
<td>2.400</td>
</tr>
<tr>
<td>Dummy Fuel</td>
<td>2.835</td>
<td>0.643</td>
<td>4.406</td>
</tr>
<tr>
<td>Dummy Fitri</td>
<td>0.543</td>
<td>0.206</td>
<td>2.639</td>
</tr>
<tr>
<td>Adjusted R-squared</td>
<td>0.992</td>
<td>S.E. of regression</td>
<td>1.047</td>
</tr>
<tr>
<td>SSR</td>
<td>358.479</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

#### Table B.
**Phillips curve with the threshold of M1 growth: third point**

<table>
<thead>
<tr>
<th>Coef</th>
<th>Std. Error</th>
<th>t-Statistic</th>
<th>Prob.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant</td>
<td>-0.387</td>
<td>0.152</td>
<td>-2.549</td>
</tr>
<tr>
<td>Inflation(-1)</td>
<td>0.684</td>
<td>0.037</td>
<td>18.475</td>
</tr>
<tr>
<td>Inflation(1)</td>
<td>0.256</td>
<td>0.052</td>
<td>4.972</td>
</tr>
<tr>
<td>Output Gap(-9)</td>
<td>0.049</td>
<td>0.021</td>
<td>2.317</td>
</tr>
<tr>
<td>Exchange Rate Dep(-1)</td>
<td>-0.045</td>
<td>0.009</td>
<td>-5.186</td>
</tr>
<tr>
<td>M1 Growth(-2) &lt;= 4.93%</td>
<td>0.085</td>
<td>0.077</td>
<td>1.097</td>
</tr>
<tr>
<td>4.93% &lt; M1 Growth(-2) &lt;= 7.08%</td>
<td>0.169</td>
<td>0.055</td>
<td>3.094</td>
</tr>
<tr>
<td>7.08% &lt; M1 Growth(-2) &lt;= 9.84%</td>
<td>0.085</td>
<td>0.030</td>
<td>2.848</td>
</tr>
<tr>
<td>9.84% &lt; M1 Growth(-2)</td>
<td>0.031</td>
<td>0.008</td>
<td>3.900</td>
</tr>
<tr>
<td>Dummy Crisis</td>
<td>1.116</td>
<td>0.498</td>
<td>2.242</td>
</tr>
<tr>
<td>Dummy Fuel</td>
<td>2.926</td>
<td>0.639</td>
<td>4.576</td>
</tr>
<tr>
<td>Dummy Fitri</td>
<td>0.600</td>
<td>0.203</td>
<td>2.963</td>
</tr>
<tr>
<td>Adjusted R-squared</td>
<td>0.992</td>
<td>S.E. of regression</td>
<td>1.034</td>
</tr>
<tr>
<td>SSR</td>
<td>348.456</td>
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